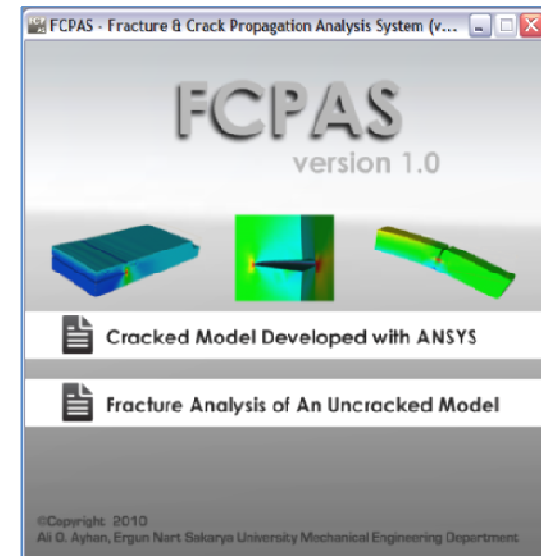
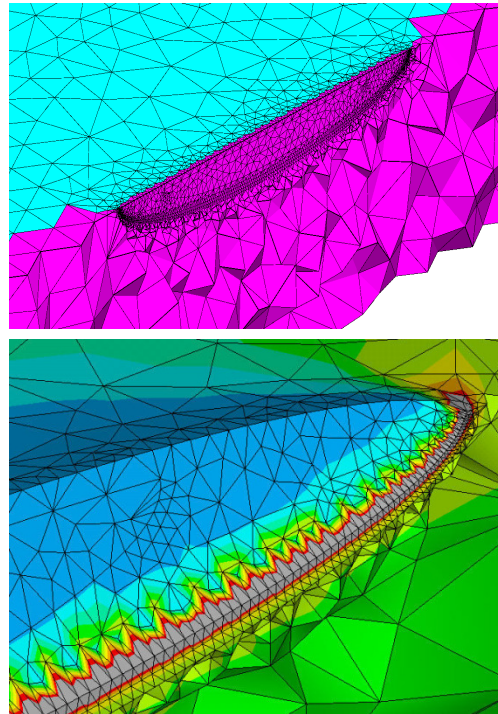
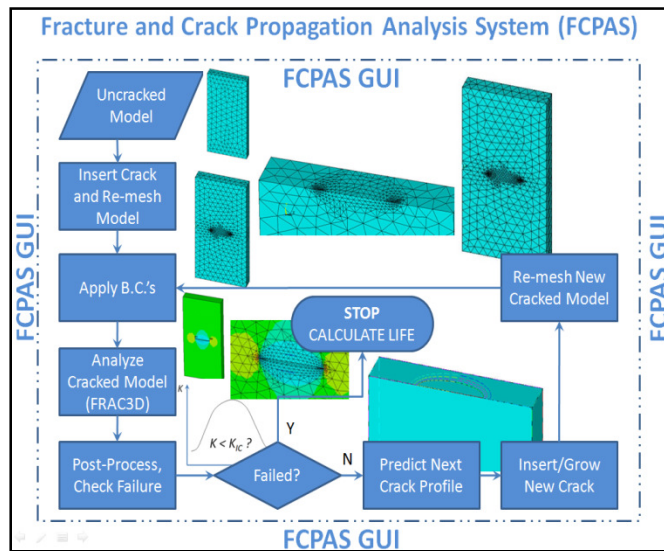


# Modeling and Analysis of Three-Dimensional Cracks Using Unstructured Finite Elements



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Sakarya University  
54187 Sakarya, TURKEY

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# Agenda

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- ❑ Fracture Mechanics – Motivation and Needs
- ❑ 3D Fracture Mechanics – Available Methods/Tools
- ❑ Enriched Finite Elements for 3D Fracture Mechanics
- ❑ FCPAS – Fracture and Crack Propagation Analysis System
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- ❑ Summary/Conclusions

# Why Fracture Mechanics?

## Schenectady T2 Tanker, January 16, 1943



- 152m long T2 tanker, 'Schenectady'
- 16 January 1943 (A few days after the sea trials)
- Breaks into two parts while lying at the harbor (Portland, Oregon)
- Still harbor water and about 4°C
- Light winds and air temperature about -3°C
- Sudden failure heard a mile away
- Fracture extended through the deck, the sides of the hull, the longitudinal bulkheads and the bottom girders.
- Central part of the ship rose clear of the water

**Poor welding in highly stressed region**

# Why Fracture Mechanics?

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## Aloha Airlines Flight 243, April 28, 1988



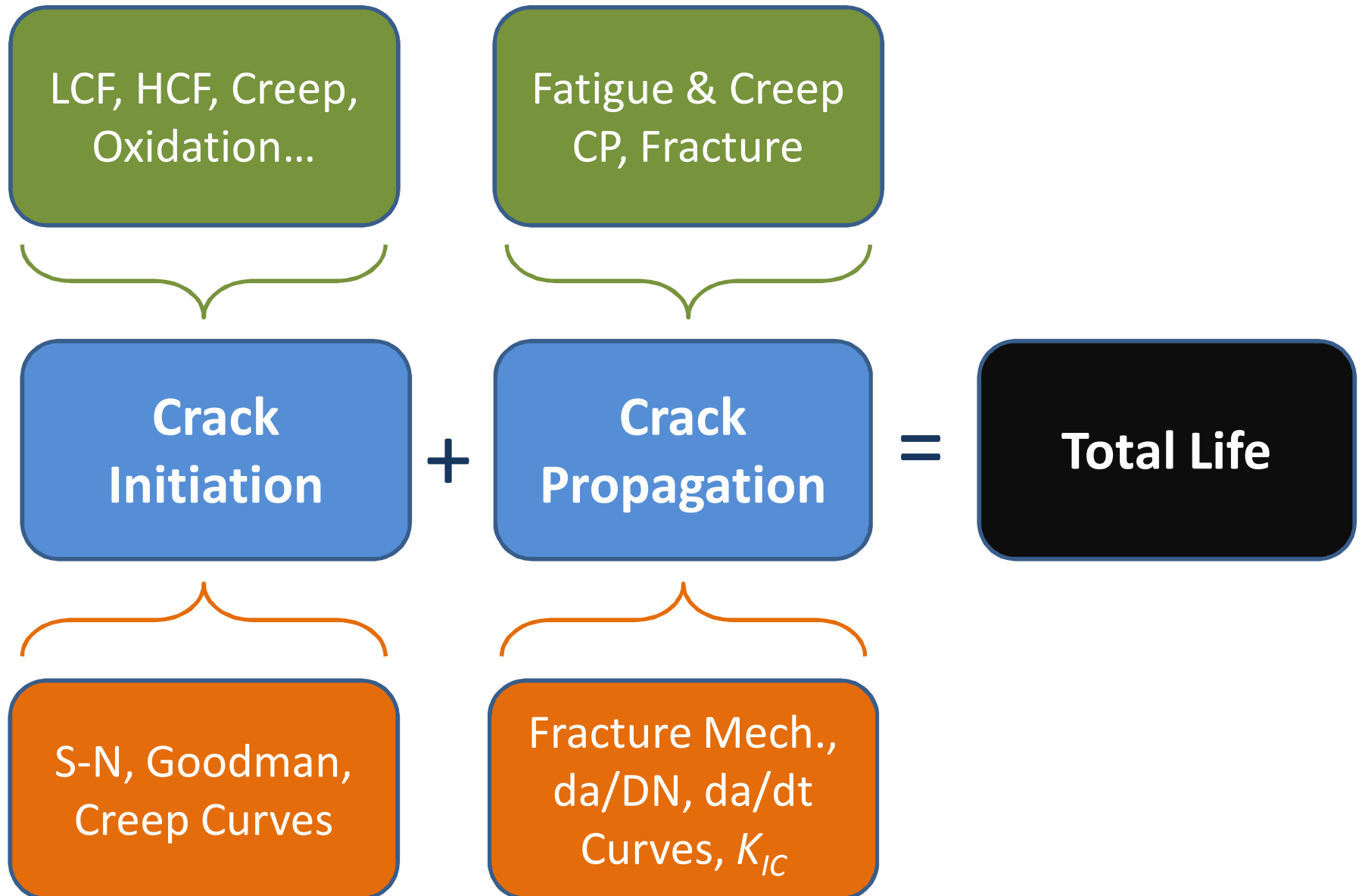
- April 28, 1988, 1:25 pm Hilo to Honolulu
- Rupture of fuselage at the top of its climb
- Senior flight attendant blown from the aircraft to her death
- The cockpit door and roof blown away
- Most passengers were injured, seven seriously

**Undetected “fatigue damage”**

**Ref:** <http://www.volpe.dot.gov/infosrc/journal/30th/safety.html>

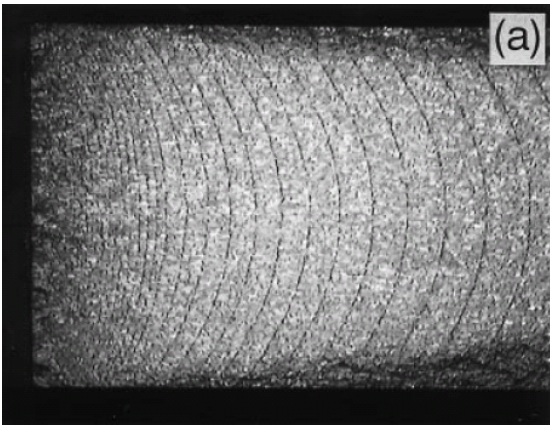
# Mechanical Life of A Part

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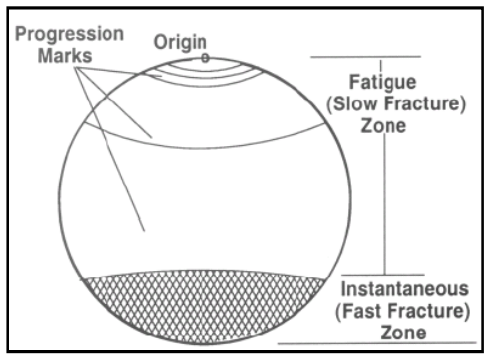


# 3D Fracture Mechanics – Motivation and Needs

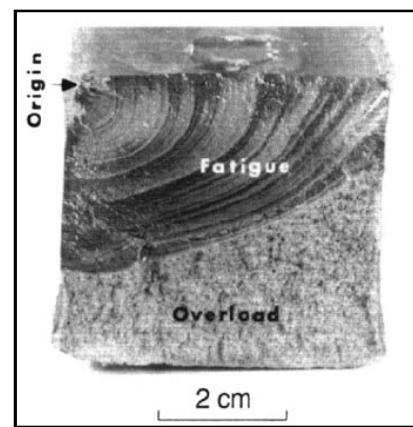
**Aluminum Plate**  
(Takashi et al, 2000)



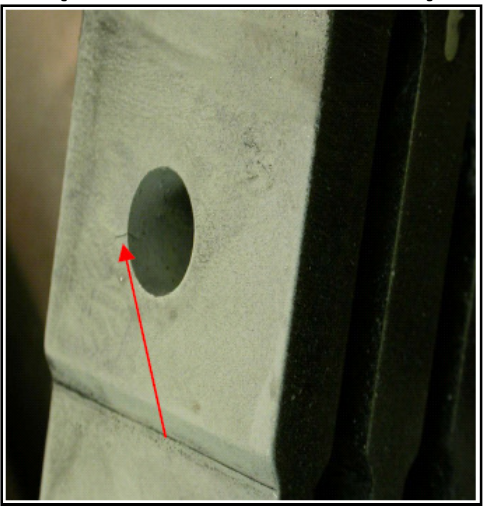
**Fatigue Crack Propagation**



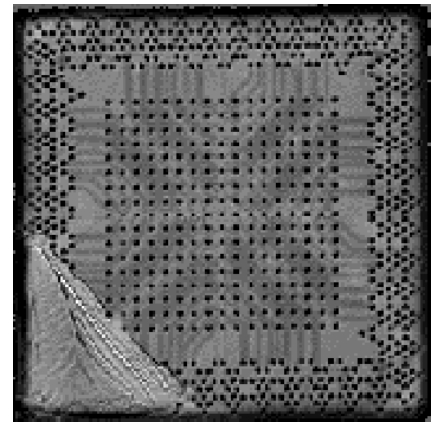
**A Machine Part**  
(Dowling, 2002)



**Turbine Bucket Dovetail**  
(Dumas et al, 2006)



**Electronic Package (D. Peterson, 1998)**



*Though many problems can be approximated by 2D methods, most real problems are 3D*

# Agenda

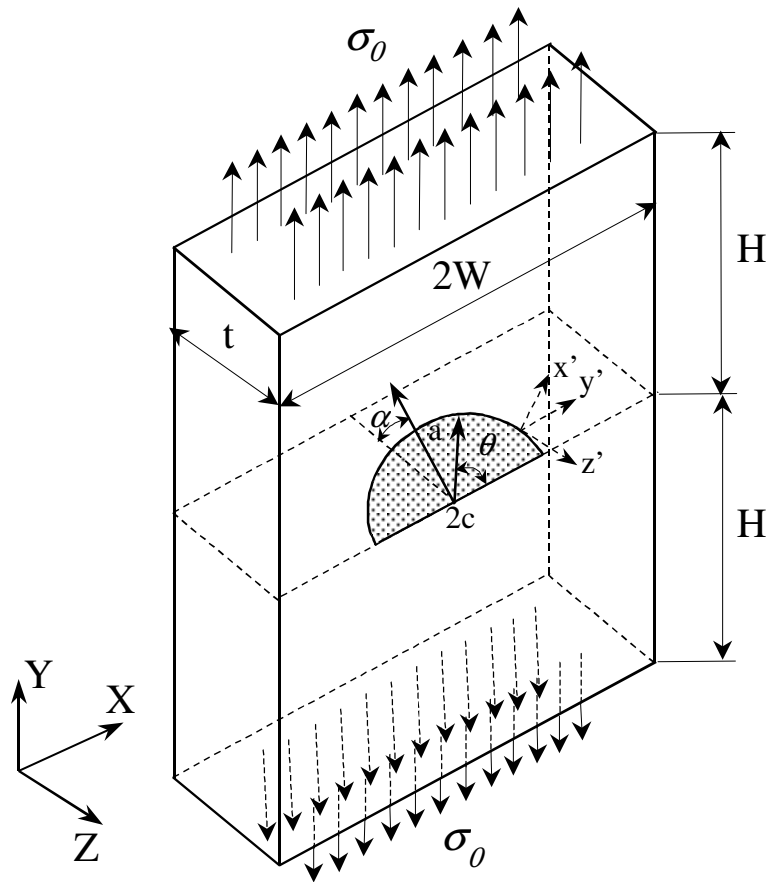
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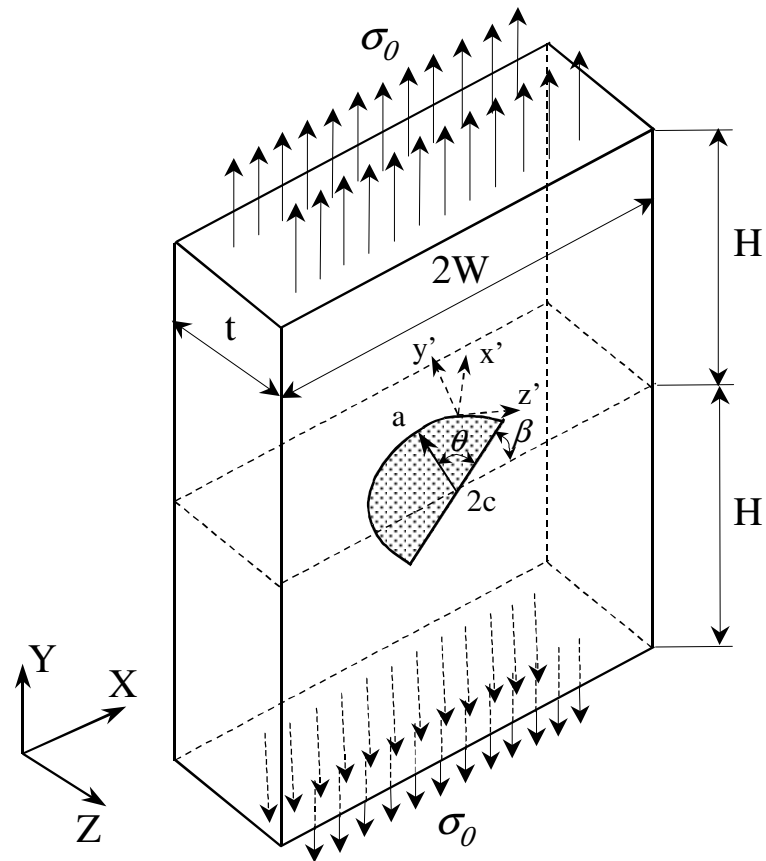
# 3D Fracture Mechanics

The Most Common Types of Cracks are Surface & Corner Cracks

Deflected Surface Crack



Inclined Surface Crack





# 3D Fracture Mechanics – Available Methods/Tools

## Disadvantages

- Limited geometry or loading

- Alternating methods
- Boundary element methods
- Virtual Crack Extension Method
- Line-Spring Method

## Advantages

- Quicker to solve, simple models and geometries

- Model and mesh generation can be time consuming

- Finite Element Methods
  - Quarter-point elements
  - J & Interaction Integral
  - Domain Integral
  - Enriched Finite Elements  
(Topic of This Presentation)

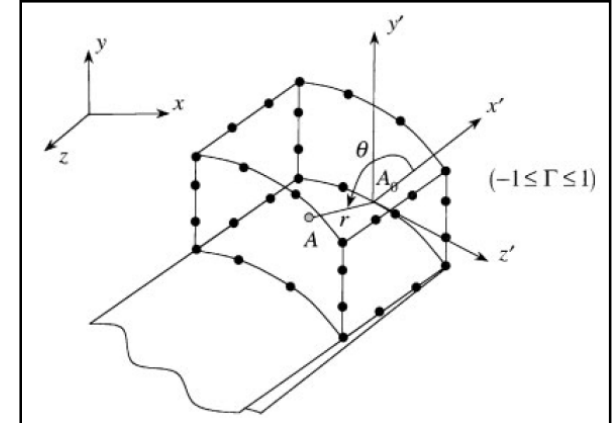
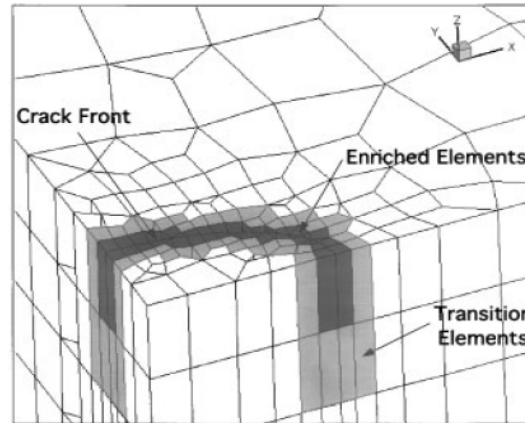
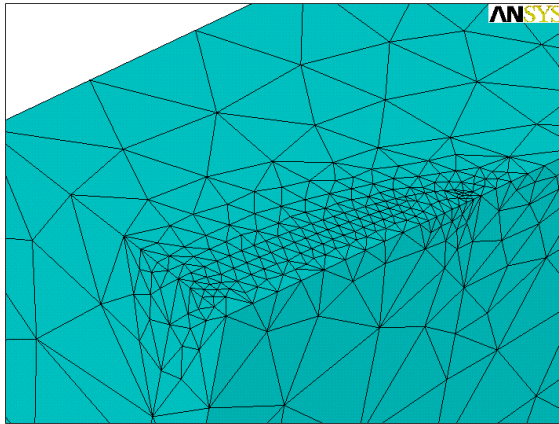
- Accurate representation of actual geometry and local loads near crack region
- *Multi-loading and material model capabilities*

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# Enriched Finite Elements for 3D Fracture Analysis



$$u(\xi, \eta, \rho) = \sum_{j=1}^{nodel} N_j(\xi, \eta, \rho) u_j + Z_0(\xi, \eta, \rho) \sum_{i=1}^{ntip} N_i(\bar{\xi}) K_I^i \left( f_1(\xi, \eta, \rho) - \sum_{j=1}^{nodel} N_j(\xi, \eta, \rho) f_{1j} \right) + Z_0(\xi, \eta, \rho) \sum_{i=1}^{ntip} N_i(\bar{\xi}) K_{II}^i \left( g_1(\xi, \eta, \rho) - \sum_{j=1}^{nodel} N_j(\xi, \eta, \rho) g_{1j} \right)$$

$$v(\xi, \eta, \rho) = \sum_{j=1}^{nodel} N_j(\xi, \eta, \rho) v_j + Z_0(\xi, \eta, \rho) \sum_{i=1}^{ntip} N_i(\bar{\xi}) K_I^i \left( f_2(\xi, \eta, \rho) - \sum_{j=1}^{nodel} N_j(\xi, \eta, \rho) f_{2j} \right) + Z_0(\xi, \eta, \rho) \sum_{i=1}^{ntip} N_i(\bar{\xi}) K_{II}^i \left( g_2(\xi, \eta, \rho) - \sum_{j=1}^{nodel} N_j(\xi, \eta, \rho) g_{2j} \right)$$

$$w(\xi, \eta, \rho) = \sum_{j=1}^{nodel} N_j(\xi, \eta, \rho) w_j + Z_0(\xi, \eta, \rho) \sum_{i=1}^{ntip} N_i(\bar{\xi}) K_{III}^i \left( h(\xi, \eta, \rho) - \sum_{j=1}^{nodel} N_j(\xi, \eta, \rho) h_j \right)$$

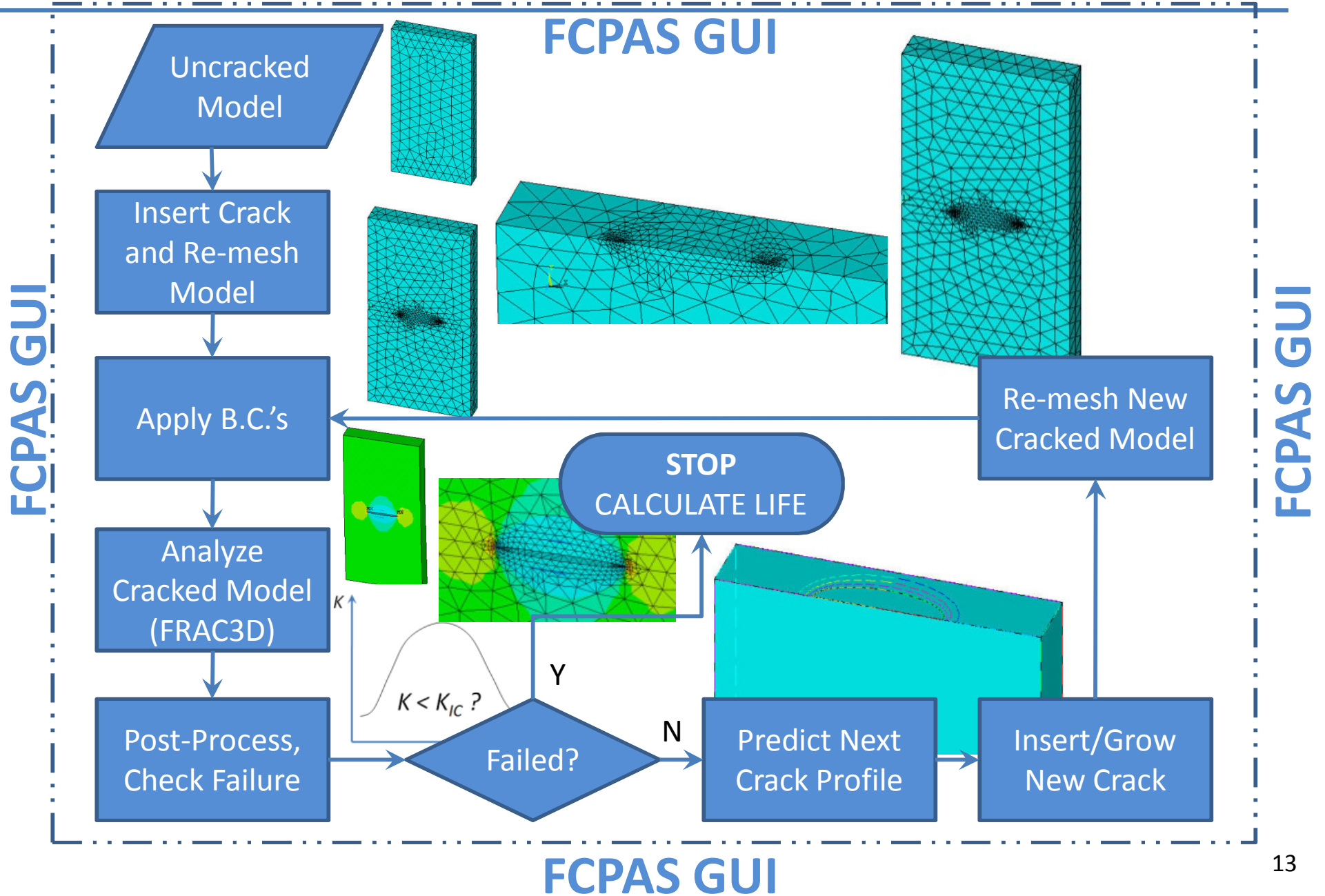
Unknown Stress Intensity Factors Are Included in the FE Formulation & Solved for Directly

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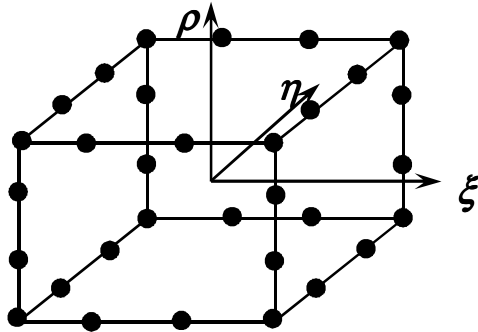
# Fracture and Crack Propagation Analysis System (FCPAS)



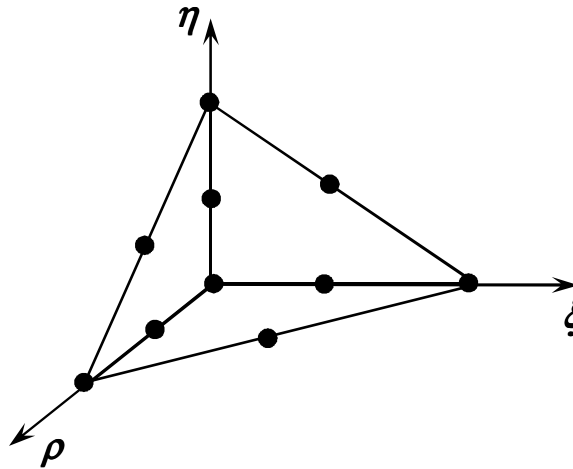
# FRAC3D – FCPAS Solver for 3D Fracture Analysis

- Supported Element Types

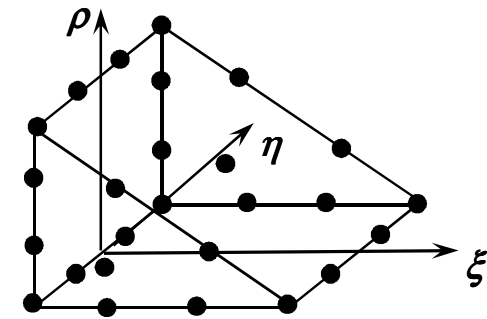
32-Node Hexahedron



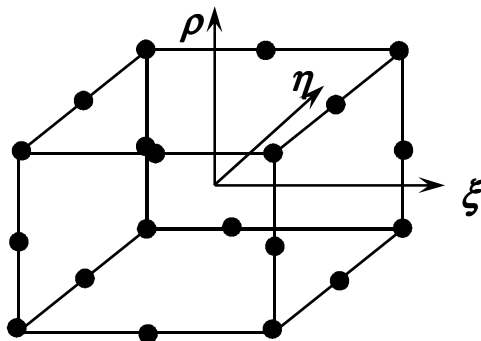
10-Node Tetrahedron



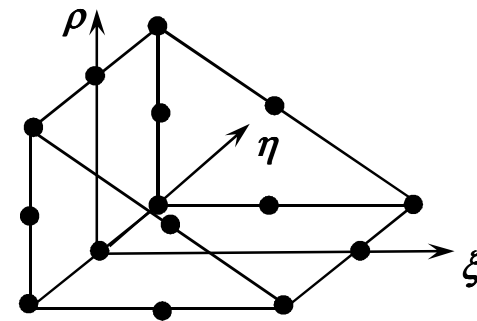
26-Node Pentahedron



20-Node Hexahedron



15-Node Pentahedron

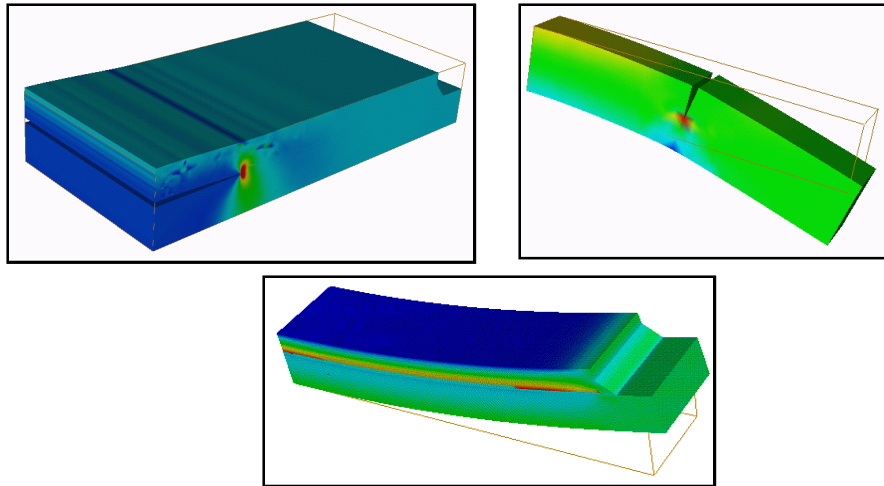


# FRAC3D – FCPAS Solver for 3D Fracture Analysis

## *Boundary Conditions*

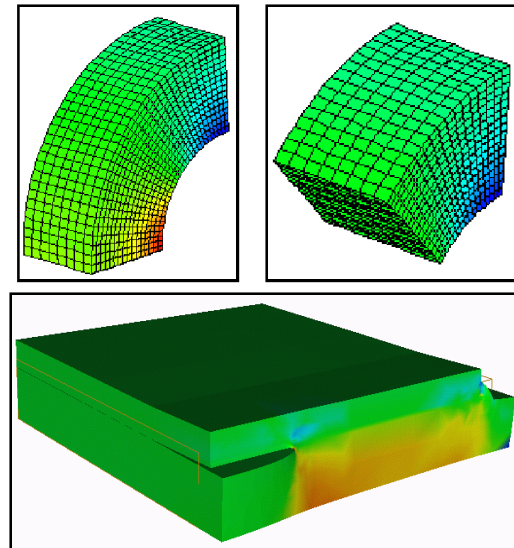
- Load Types

- Pressure Loading on Surfaces
- Concentrated Forces on Nodes
- Thermal Loading
- Inertia Loading
- Centrifugal Loading



- Constraints

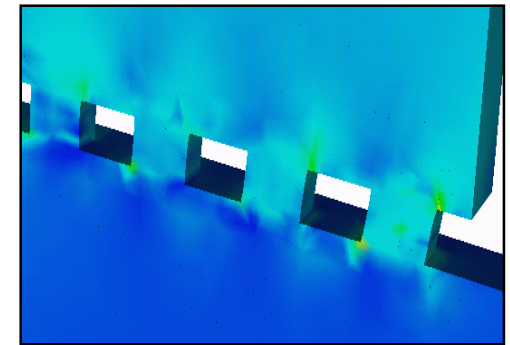
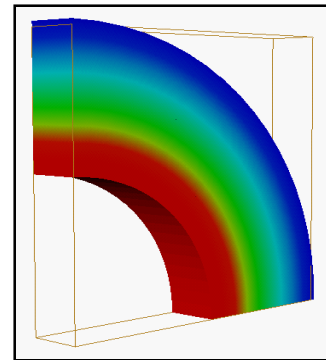
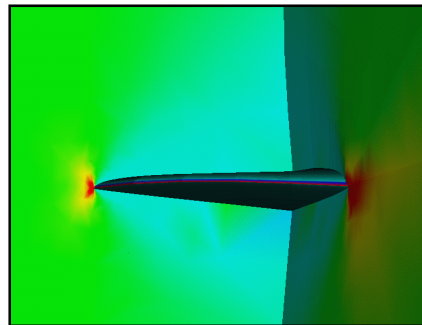
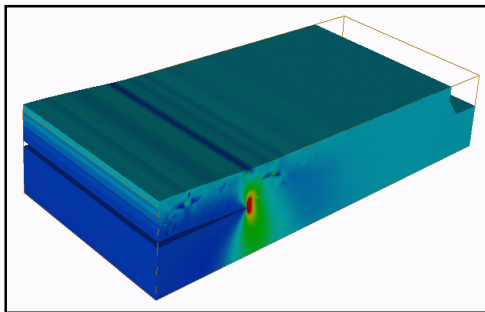
- Displacement Constraints on Nodes
- Constraints on Node Sets (Tied Nodes)
- Displacements on Skew Edges
- Sub-model BC's from ANSYS



# FRAC3D – FCPAS Solver for 3D Fracture Analysis

## *Analysis Types & Material Systems Supported*

- Analysis Types
  - Elastic Stress Analysis
  - Elastic/Plastic Stress Analysis
  - Linear Elastic Fracture Mechanics w/ & w/o plasticity on uncracked material
  - Submodeling of ANSYS models
- Material Systems
  - Homogeneous Isotropic
  - Bi-material Isotropic
  - Homogeneous Orthotropic
  - FGM Isotropic
  - Elastic/plastic Isotropic





# Agenda

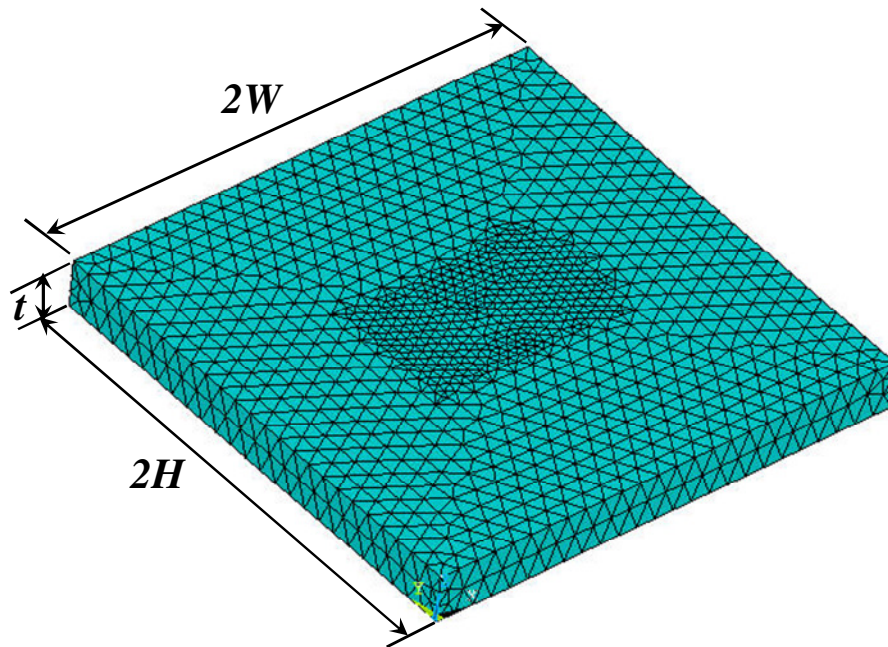
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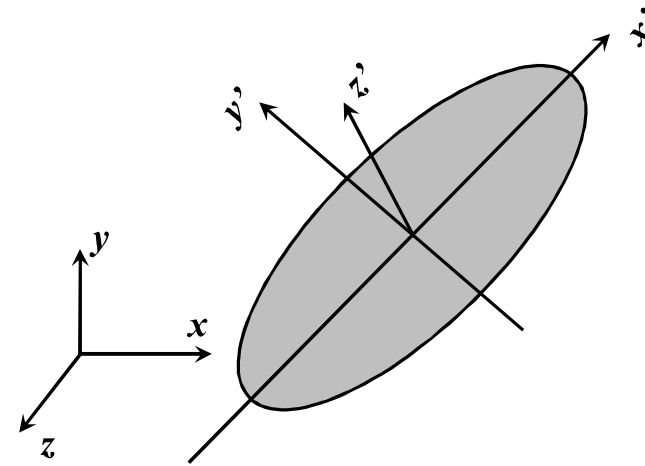
# Applications: Crack Insertion (Mode-I Surface Crack)

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Uncracked Plate Finite Element Model



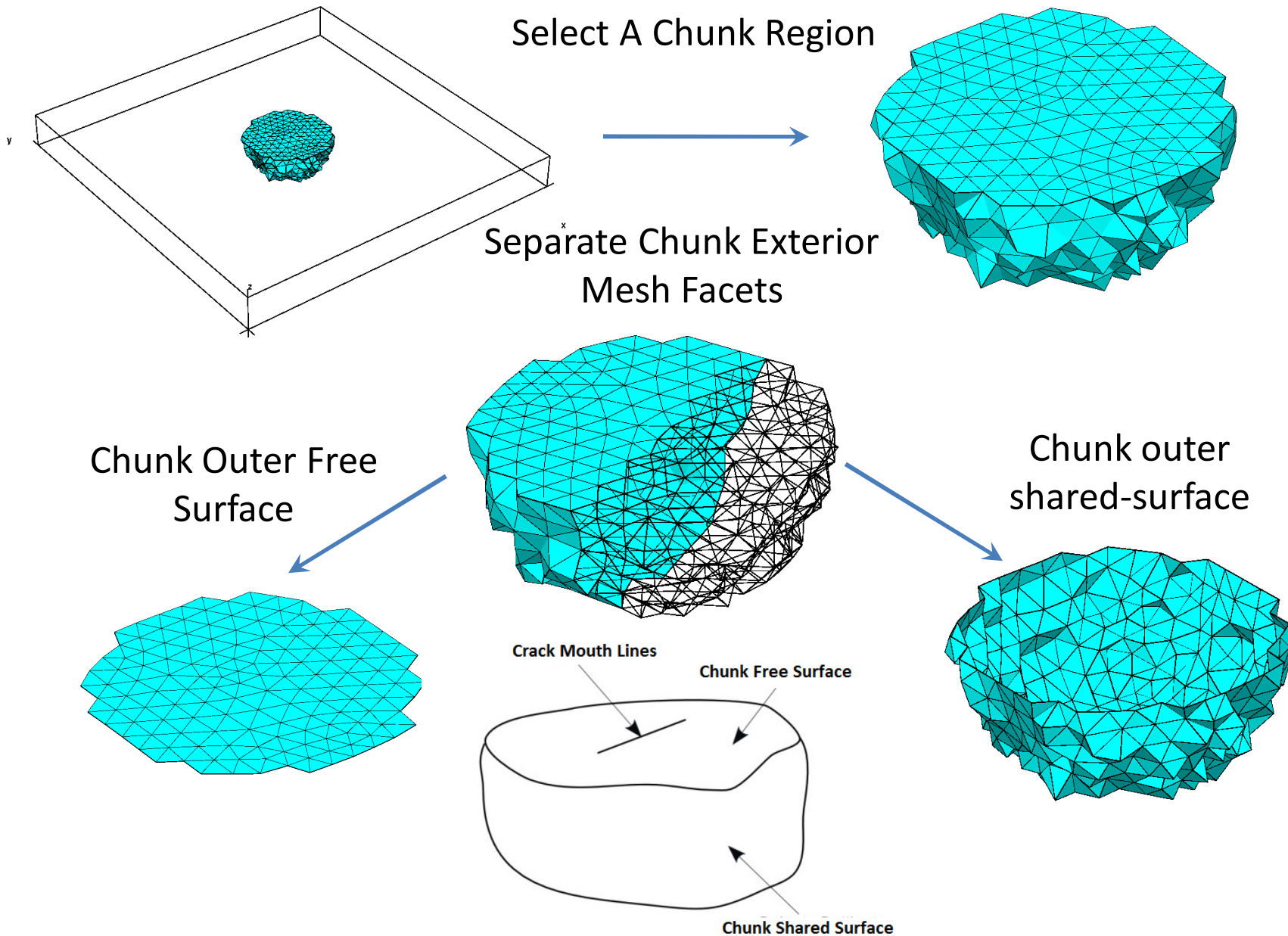
An Elliptical Crack Shape to be Inserted into Plate Model



Info for ...

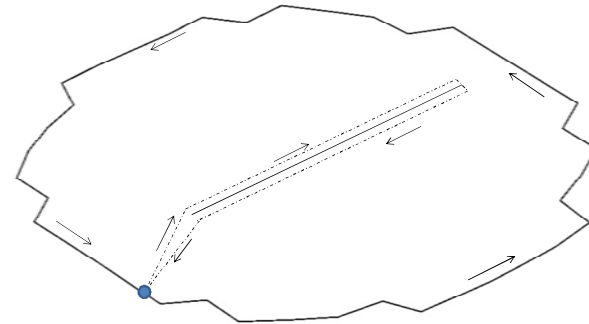
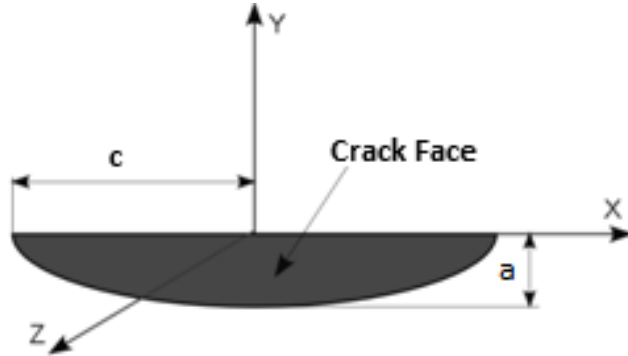
***Location, Size and Orientation***  
of the crack are needed !

# Applications: Crack Insertion (Mode-I Surface Crack)

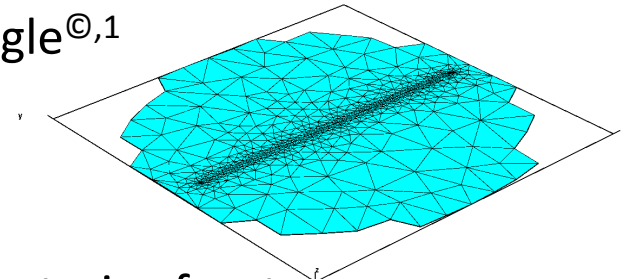
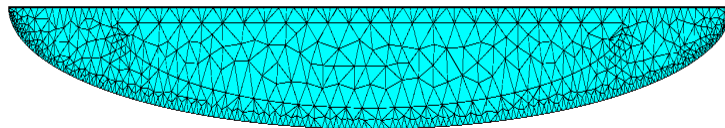


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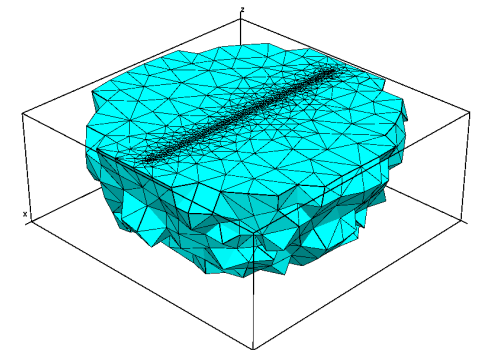
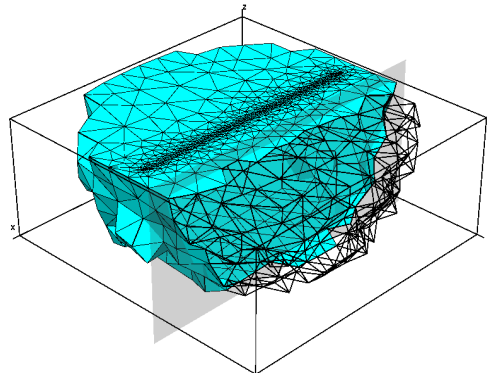
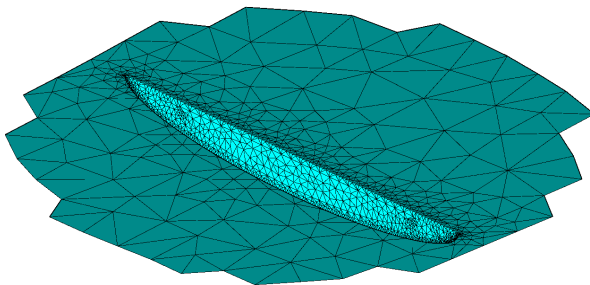
Combination of the crack mouth line and crack front line



2D meshing by Triangle<sup>©,1</sup>



Combine the modified chunk exterior facets

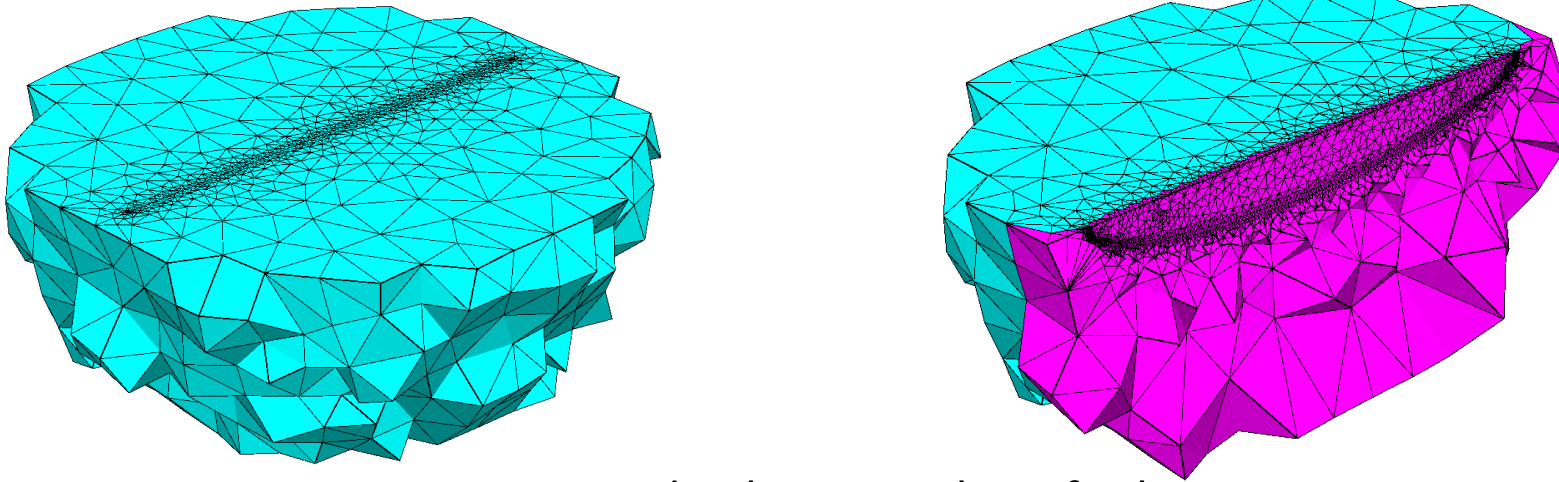


©,1 Shewchuk, J.R., 1996. Triangle: engineering a 2D quality mesh generator and Delaunay triangulator. In: Ming C., Dinesh M, editors. Applied computational geometry: towards geometric engineering. Springer-Verlag. 1148, pp. 203-222.

# Applications: Crack Insertion (Mode-I Surface Crack)

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3D meshing of Chunk Domain by Tetgen<sup>©,2</sup>



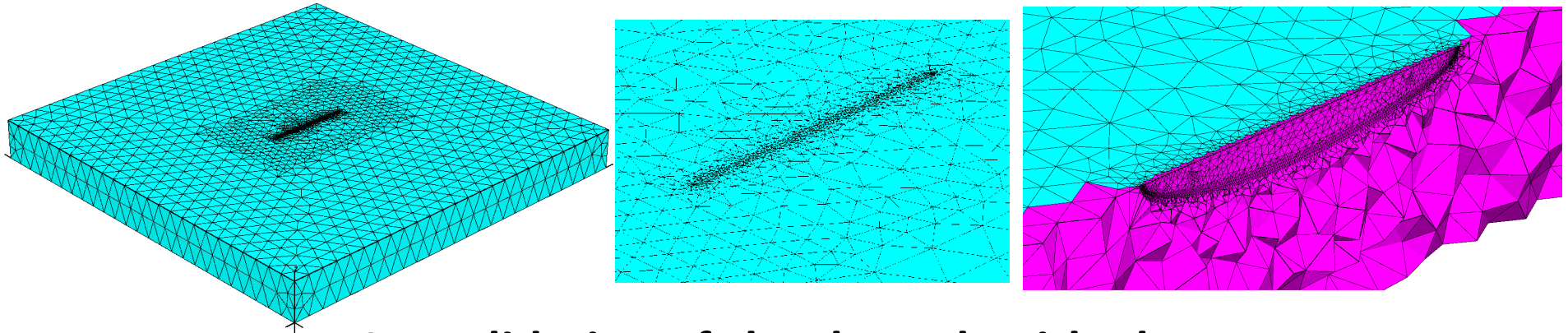
Constrained volume meshing for keeping,

- chunk outer surface facets,
- crack surfaces meshing by Triangle ©, and
- crack mouth-line nodal points

unchanged.

# Applications: Crack Insertion (Mode-I Surface Crack)

Consolidation of chunk volume mesh by Tetgen<sup>©</sup> with plate without the chunk



## Consolidation of chunk mesh with plate,

- node numbers on the shared surfaces kept the same,
- displacement and load boundary conditions outside chunk zone book kept,
- nodes on the crack surfaces duplicated and surface split,
- nodes and elements along crack front book kept to define the local crack front geometry.

**The fully-unstructured finite element mesh w/ crack included ( $a/t=0.2$ ,  $a/c=0.2$ )  
(Next step Fracture Analysis by 3D Enriched Elements)**

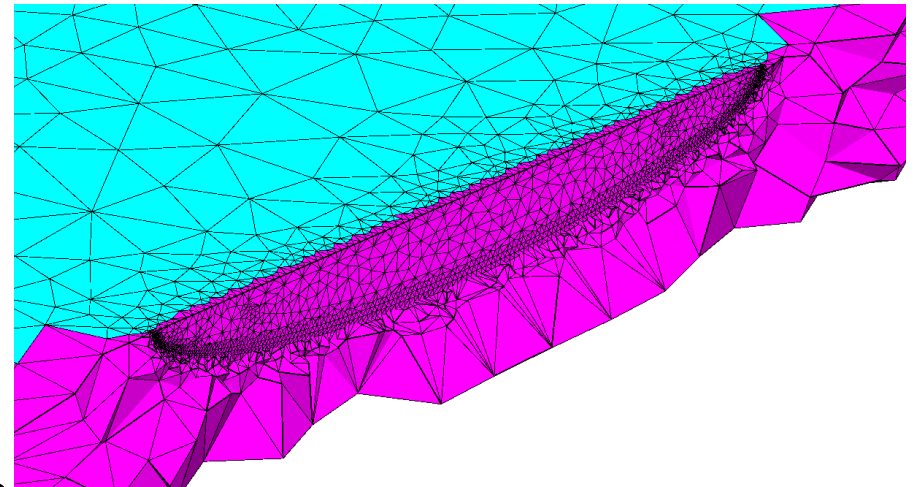
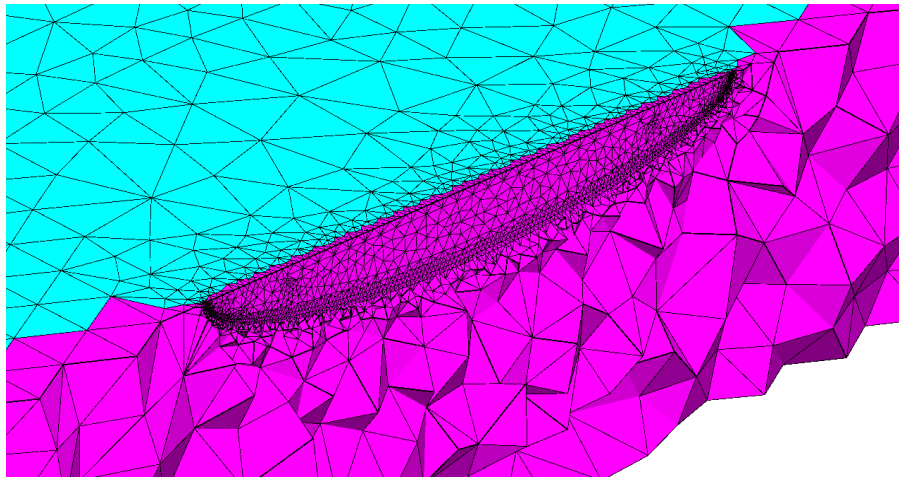
# Applications: Crack Insertion (Mode-I Surface Crack)

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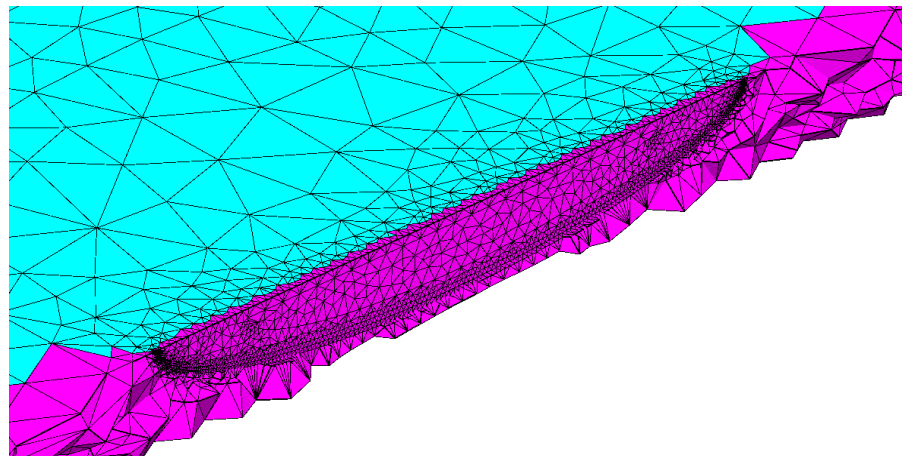
$a/c=0.2$

$a/t=0.2$

$a/t=0.5$



$a/t=0.8$

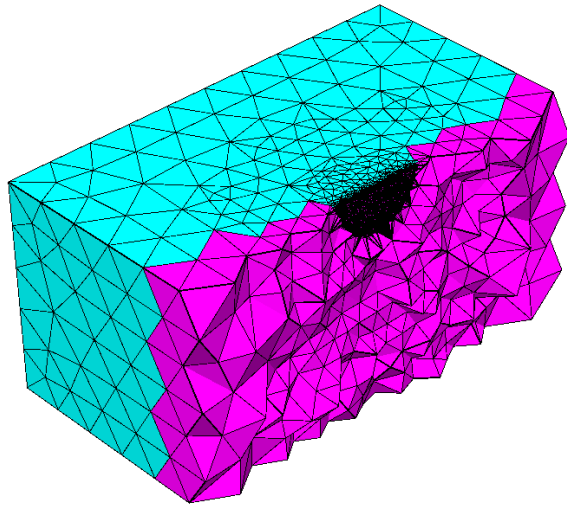


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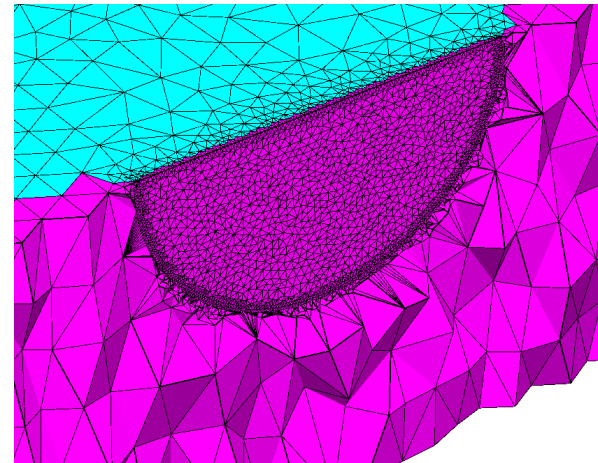
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$a/c=1.0$

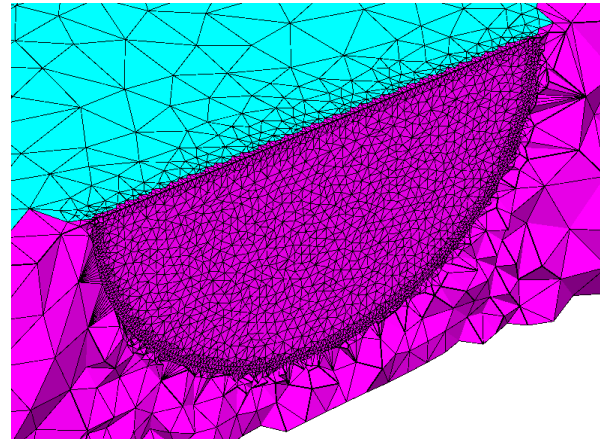
$a/t=0.2$



$a/t=0.5$



$a/t=0.8$



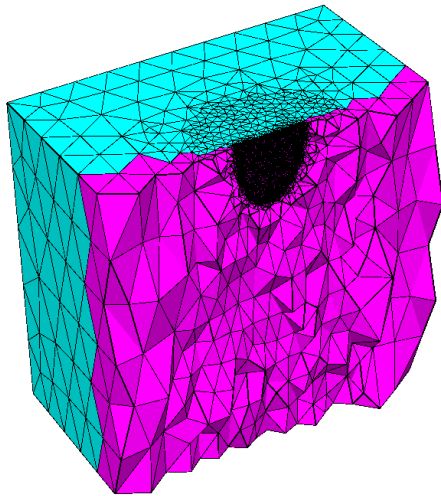


# Applications: Crack Insertion (Mode-I Surface Crack)

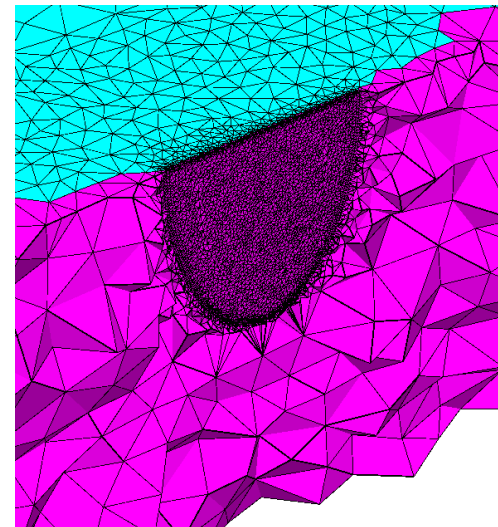
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$a/c=2.0$

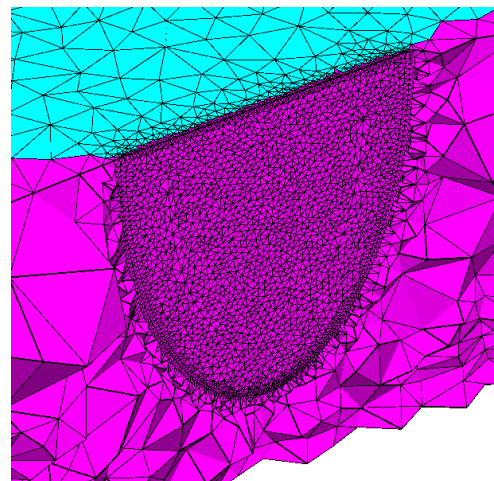
$a/t=0.2$



$a/t=0.5$

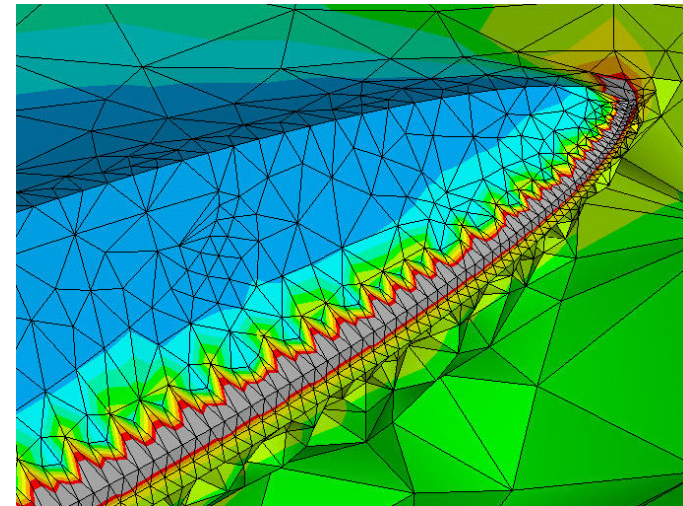
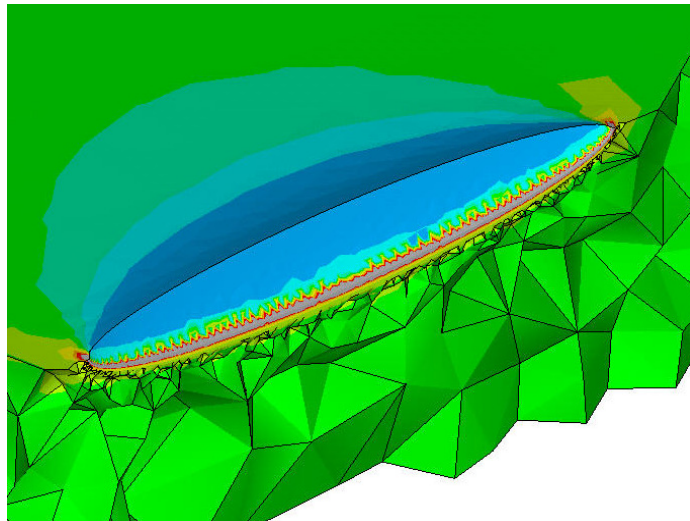
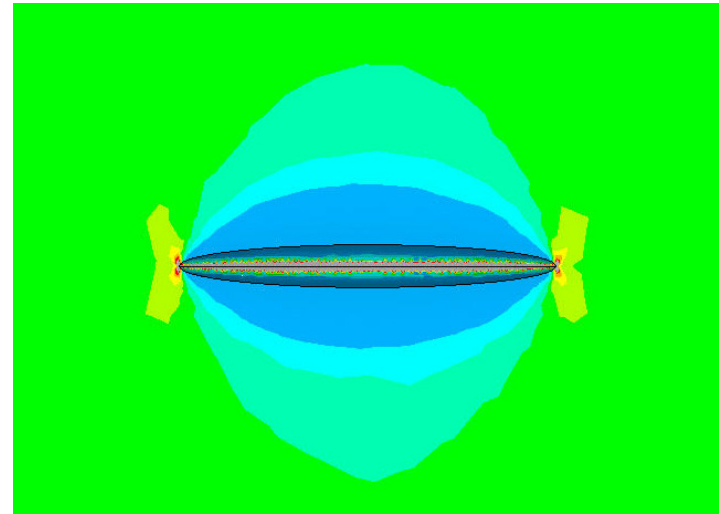
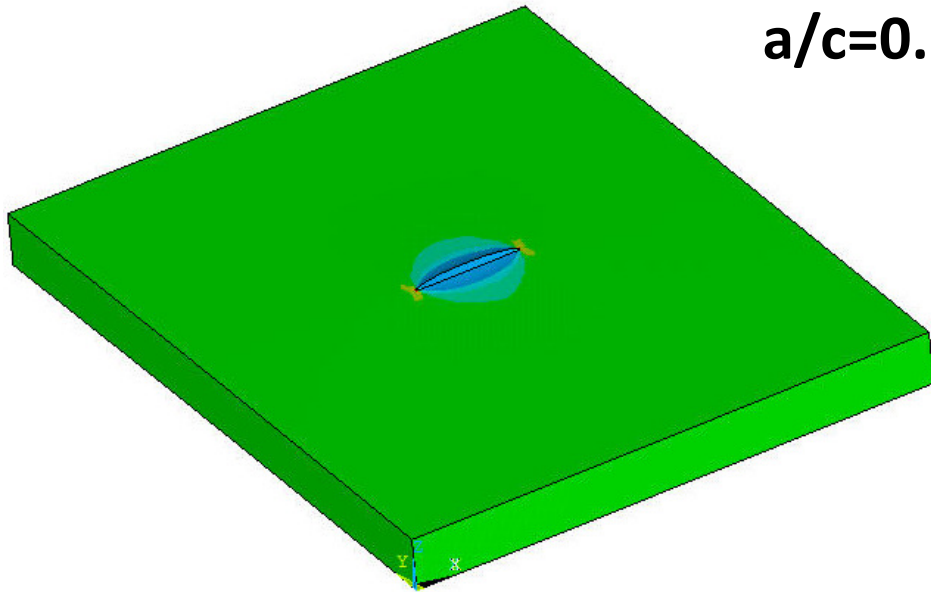


$a/t=0.8$



# Applications: Crack Insertion (Mode-I Surface Crack)

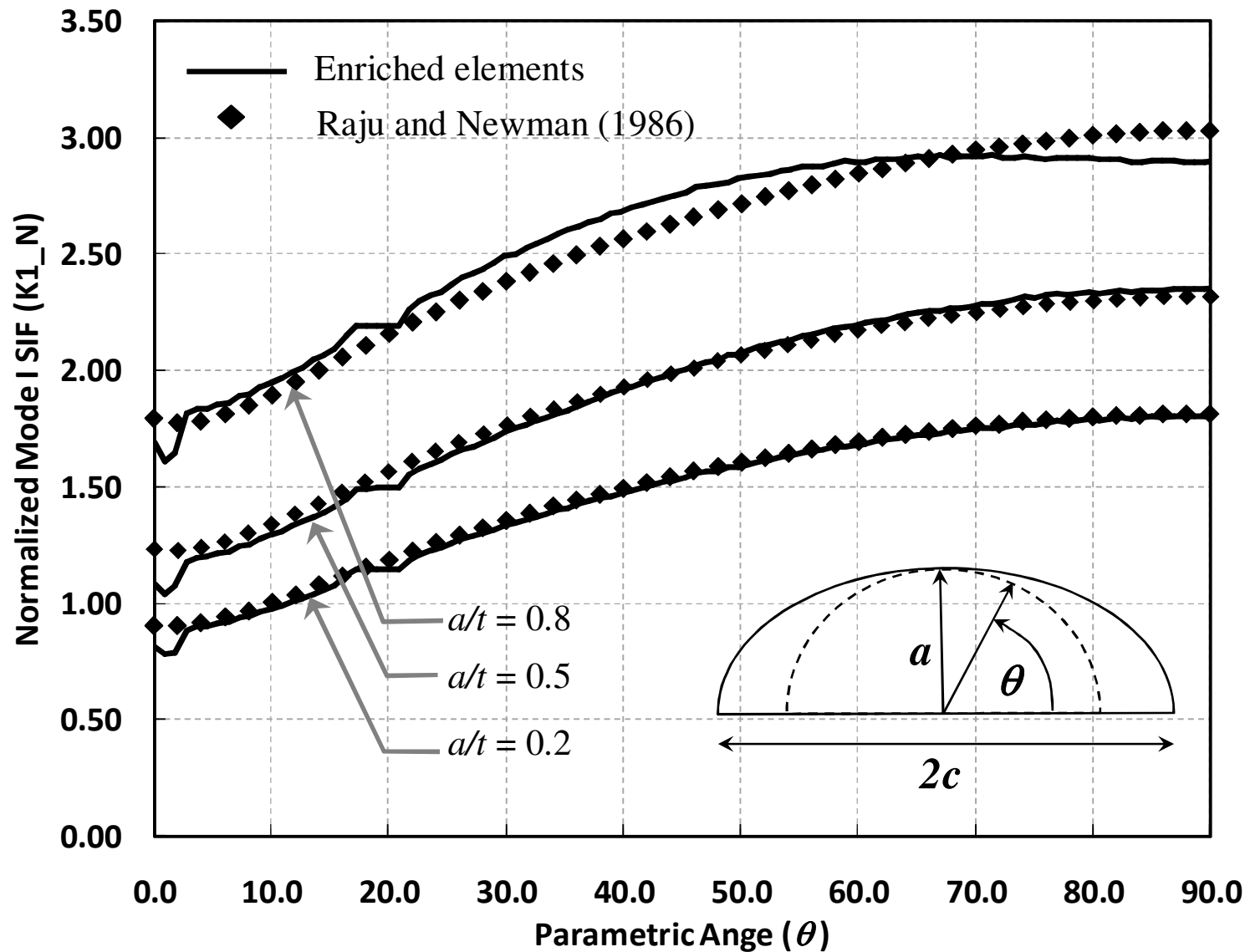
$a/c=0.2$



Deformed shapes as a first-step validation of the mesh

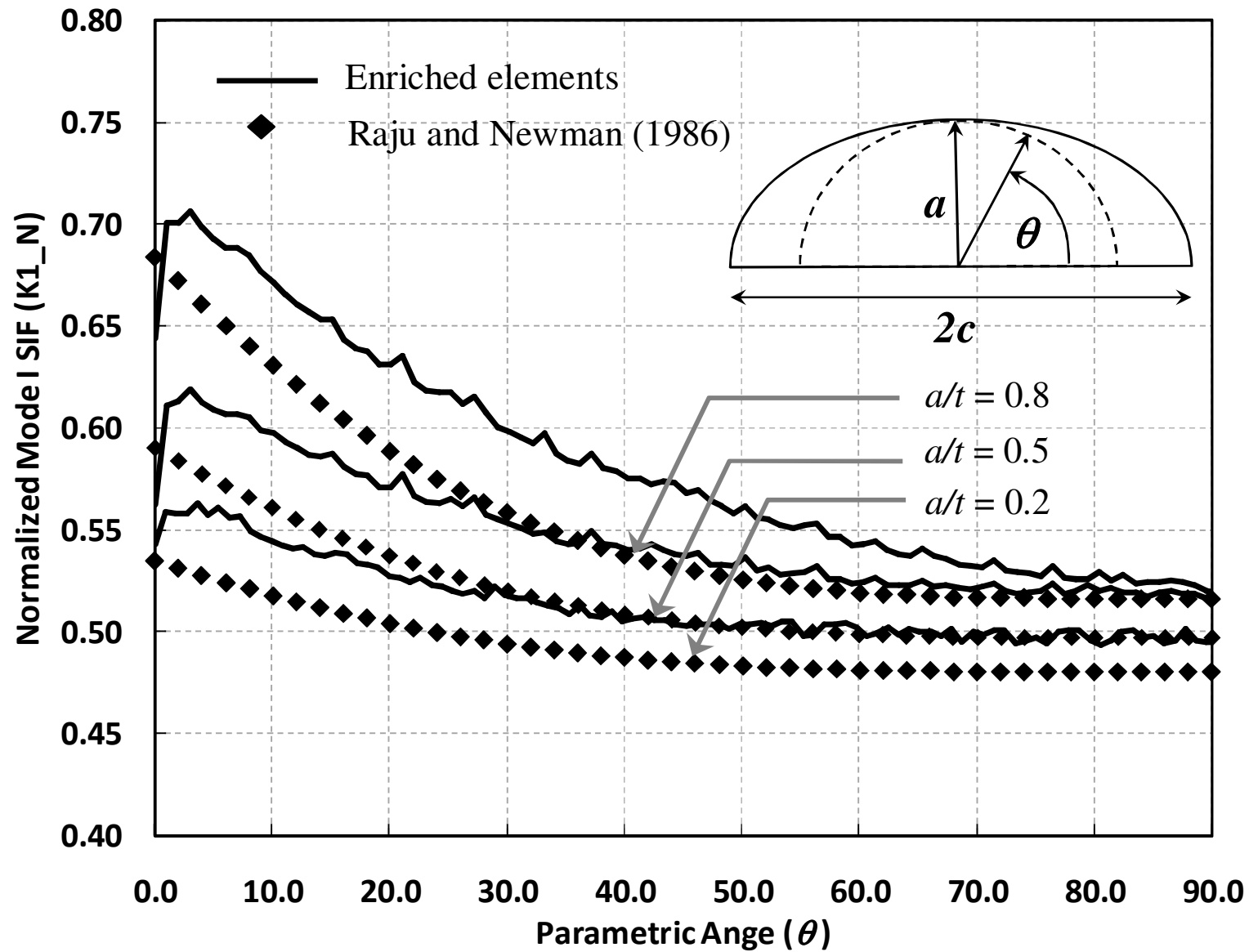
# Applications: Fracture Analysis (Mode-I Surface Crack)

$a/c=0.2$

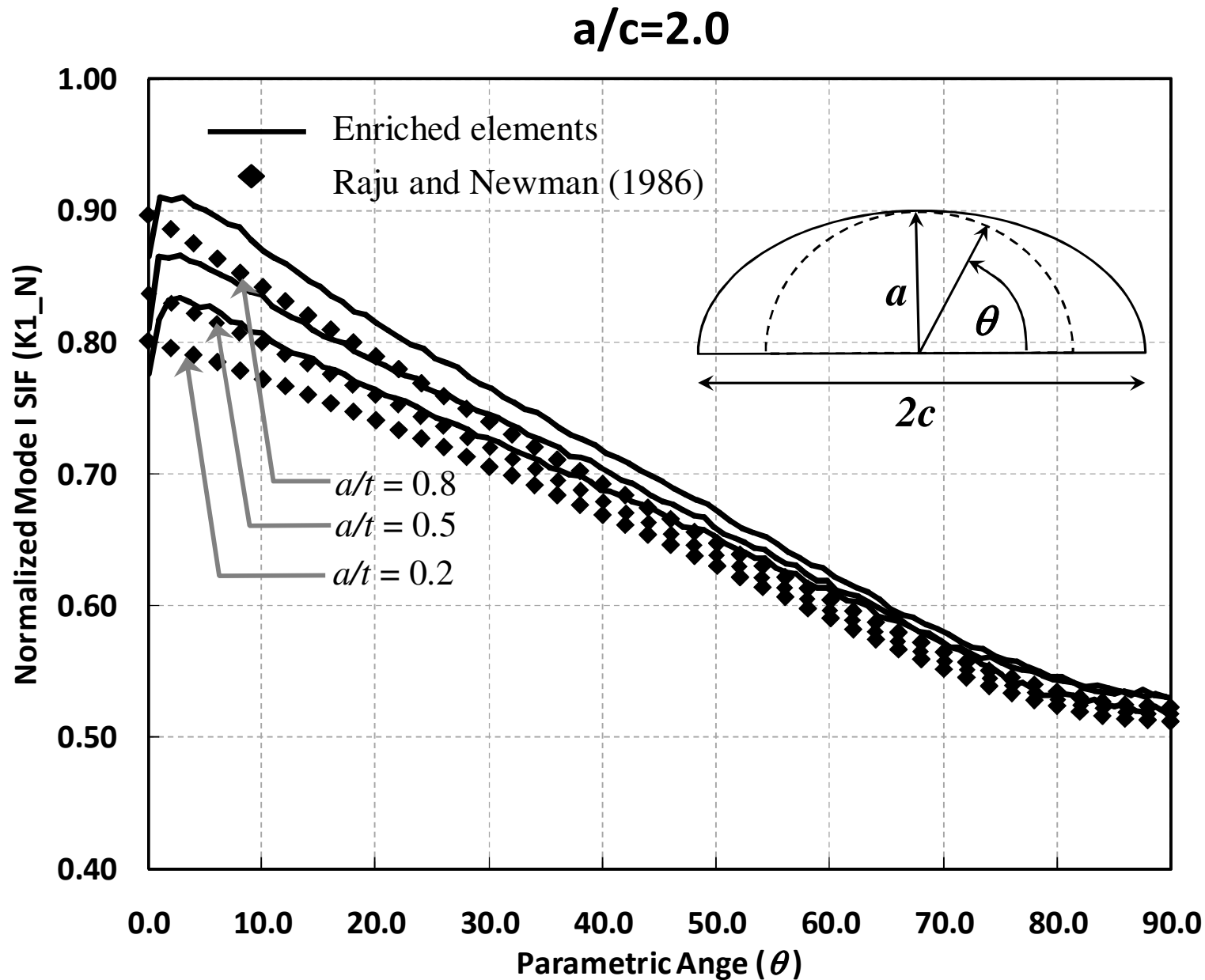


# Applications: Fracture Analysis (Mode-I Surface Crack)

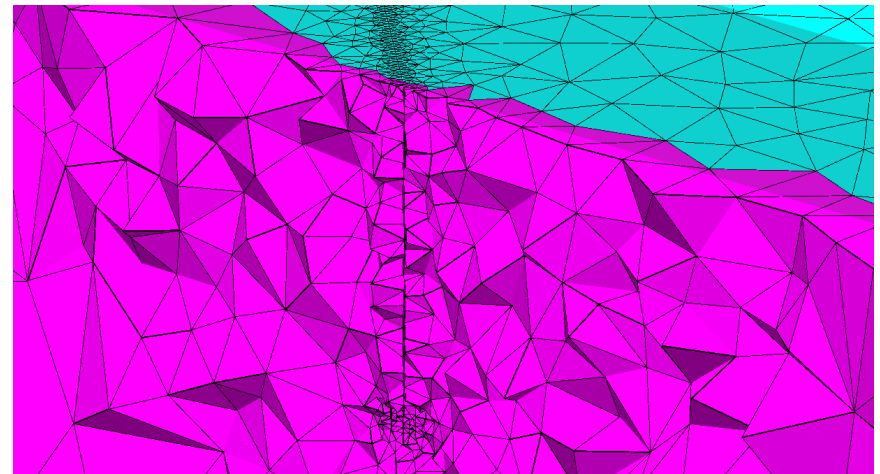
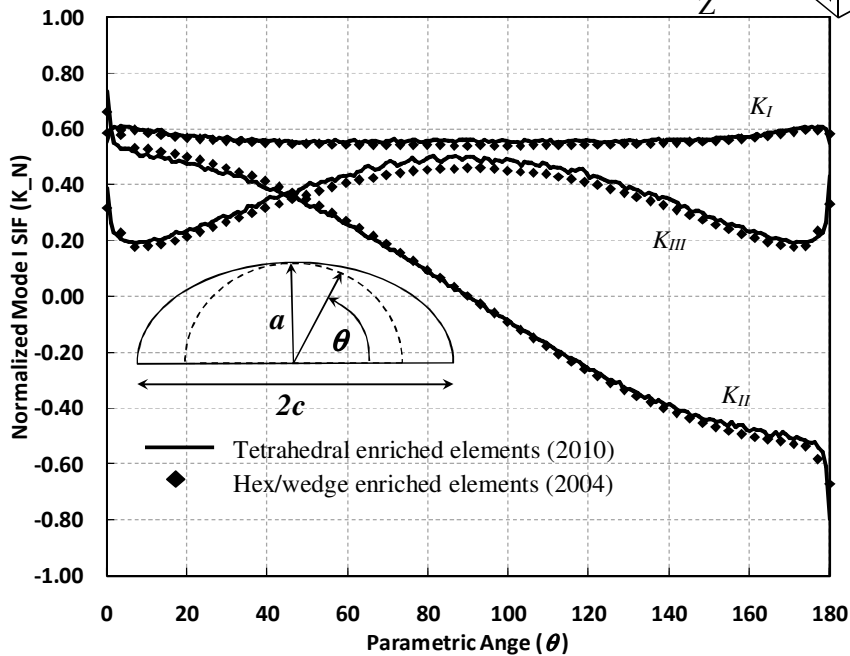
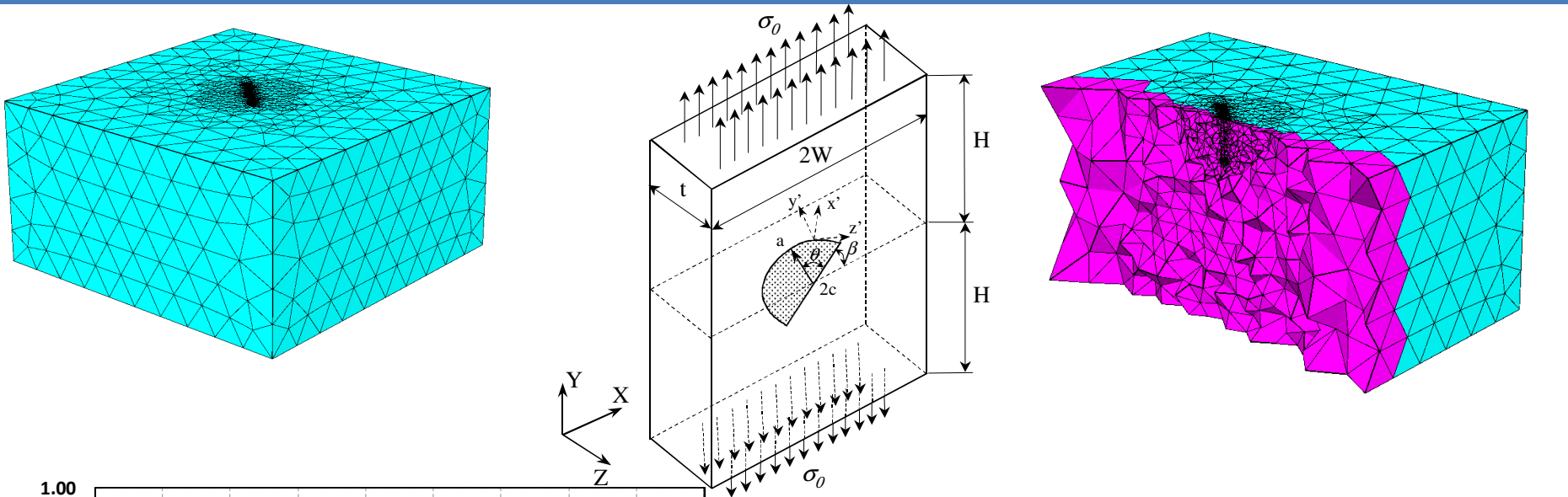
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# Applications: Fracture Analysis (Mode-I Surface Crack)

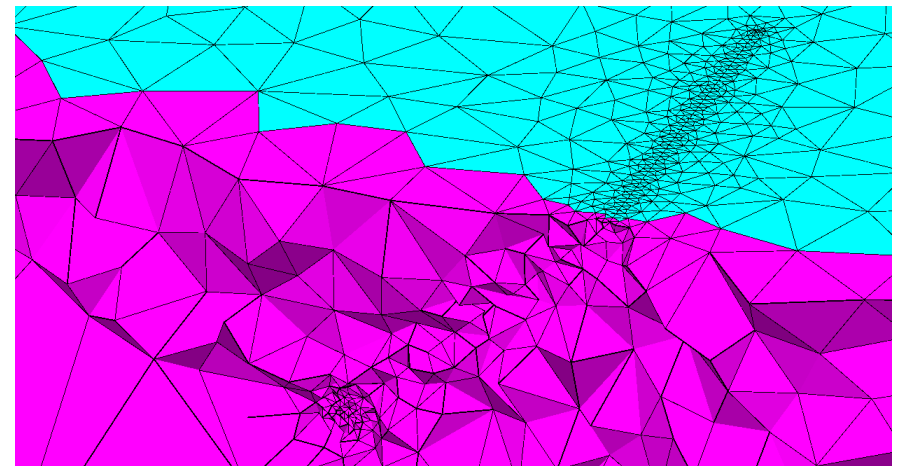
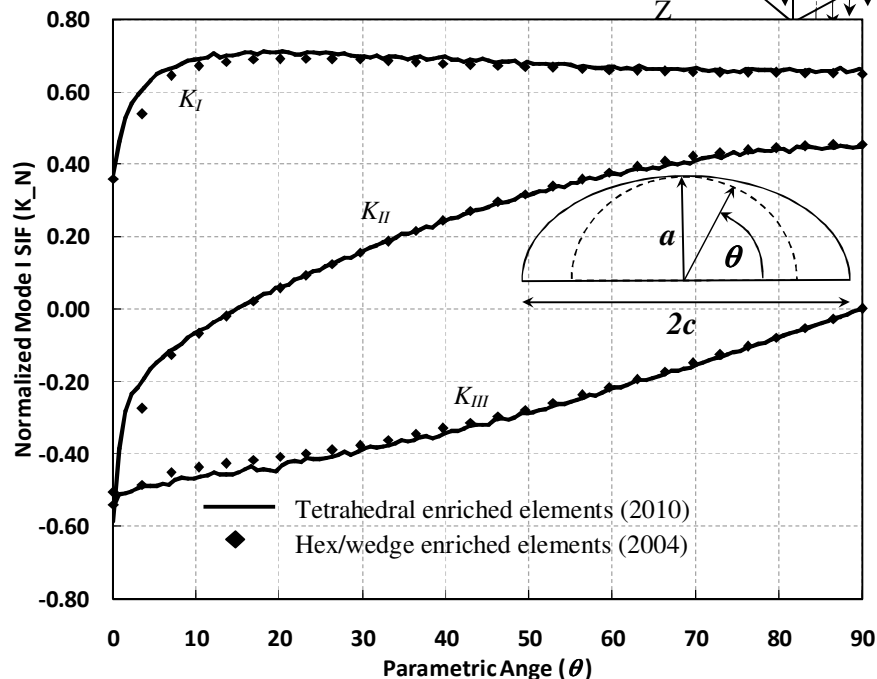
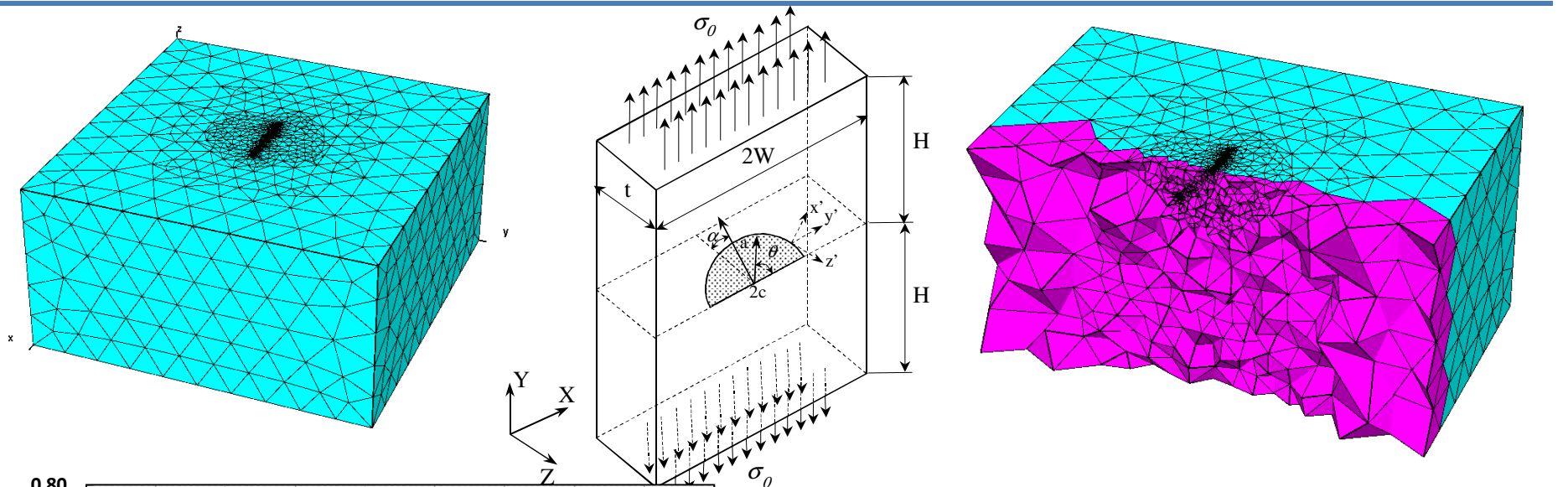


# Applications: Crack Insertion (Inclined Surface Crack)



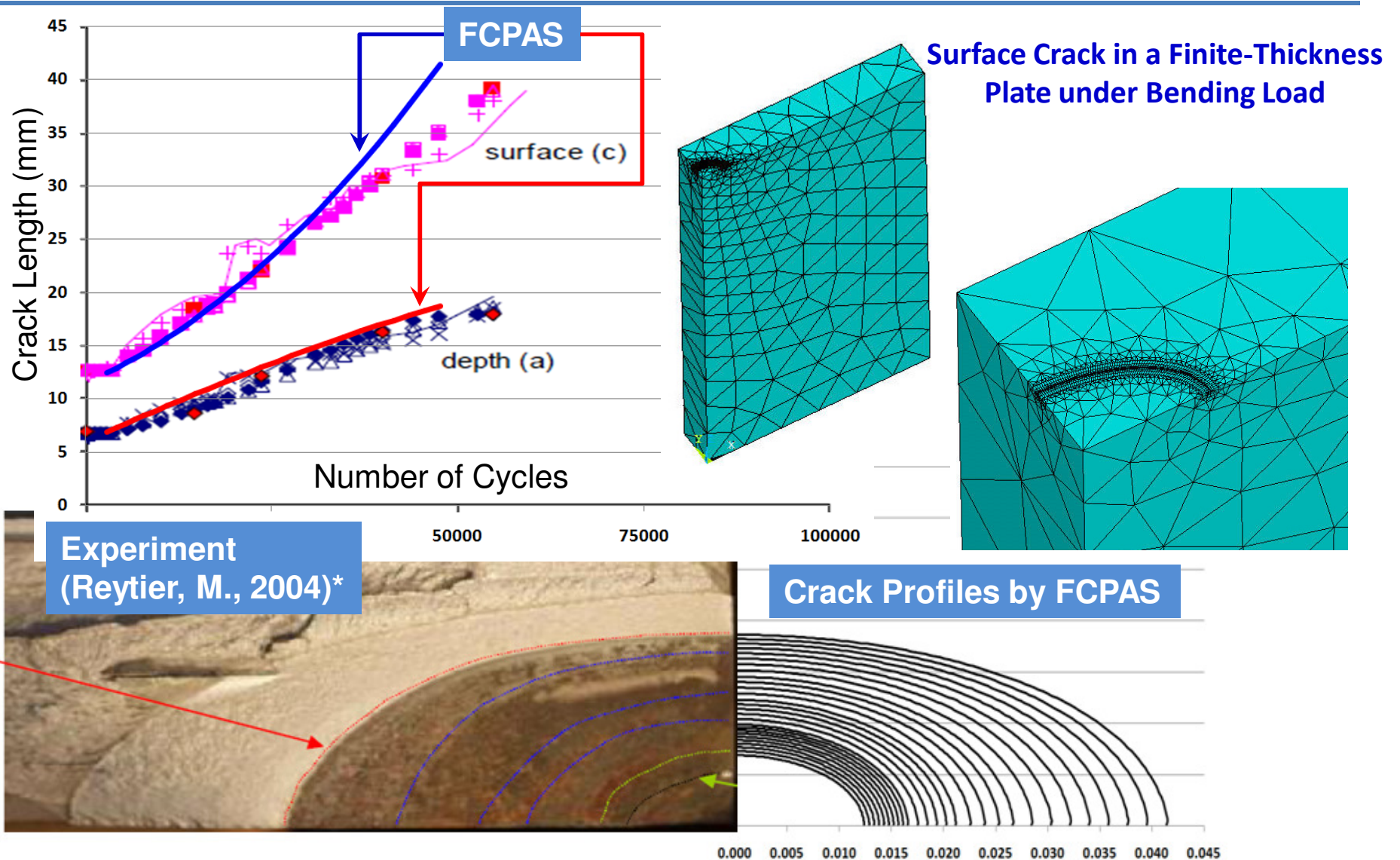
Results by Tetrahedral Enriched Elements agree with those of Hexahedral Enriched Elements (2004) <sup>30</sup>

# Applications: Crack Insertion (Deflected Surface Crack)



Results by Tetrahedral Enriched Elements agree with those of Hexahedral Enriched Elements (2004) <sup>31</sup>

# FCPAS Fatigue Crack Propagation Analysis (FE Models by ANSYS™)



FCPAS Simulation Results Agree Very Well with Experimental Observations

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# Agenda

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- ❑ Fracture Mechanics – Motivation and Needs
- ❑ 3D Fracture Mechanics – Available Methods/Tools
- ❑ Enriched Finite Elements for 3D Fracture Mechanics
- ❑ FCPAS – Fracture and Crack Propagation Analysis System
  - ❑ *Fracture finite element models developed using ANSYS*
  - ❑ *Fracture finite element models developed by crack insertion into an uncracked model*
  - ❑ *Fracture analysis by three-dimensional enriched finite elements*
- ❑ Applications:
  - ❑ *Mode-I surface crack insertion into an uncracked finite-thickness plate*
  - ❑ *Inclined and deflected surface crack insertion into an uncracked finite-thickness plate*
  - ❑ *Fracture solutions by enriched finite elements*
  - ❑ *Fatigue crack growth analysis of Mode-I surface crack in a plate under cyclic bending load*
- ❑ Summary/Conclusions

# Summary/Conclusions

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## ■ Crack Insertion into an Uncracked Finite Element Model Using Fully Unstructured Mesh

Successfully Demonstrated,

- ✓ 2D Meshing Triangle ©, 3D Meshing by Tetgen ©
- ✓ Crack insertion procedure presented by in-house code,
- ✓ Output model with fully tetrahedral finite elements to be analyzed by FCPAS Solver

## ■ Finite Element-Based Fracture Analysis Using Tetrahedral Enriched Elements,

- ✓ Fracture finite element model from crack insertion readily available for fracture analysis (\*.geo file),
- ✓ Three-dimensional enriched finite elements for fracture calculations,
- ✓ No special mesh requirements other than customary refinement near crack front,
- ✓ Stress intensity factors along crack front directly calculated at the same time as nodal displacements,
- ✓ Accurate solutions without any post-processing of finite element solution,
- ✓ Presented method very efficient as any model can be meshed with tetrahedral elements.

## ■ Crack insertion, meshing and fracture analyses of parts with curved outer surfaces next steps.

# Acknowledgements

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